

# 7.5 Factor Special Polynomials

Review:

- 1) Factor out the GCF: Always do this 1<sup>st</sup> !!
- 2) Factor by Grouping: 4 terms
- 3) Factor Trinomials: Find the factors of the last # & Add up equals the middle # (Easy)  
(a=1)
- 4) Factor Trinomials: Step 1: 2 columns  
(a ≠ 1) Step 2: Cross multiply & Add = middle #

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5) Factor special polynomials:

Ex 1)  $x^2 - 9$  must be minus !!  
↑     ↑  
square square

Special Binomial:  
difference of 2 squares.

$$= (x + 3)(x - 3)$$

split the 1<sup>st</sup> term      $\sqrt{9} = 3$

$$\text{Ex 2) } x^2 - 81y^2 = (x + \overbrace{9y}^{\sqrt{81}})(x - \overbrace{9y}^{\sqrt{81}})$$

$$\text{Ex 3) } 25x^4 - 49y^4 = (\overbrace{5x^2}^{\sqrt{25}} + \overbrace{7y^2}^{\sqrt{49}})(\overbrace{5x^2}^{\sqrt{25}} - \overbrace{7y^2}^{\sqrt{49}})$$

Ex 4)  $a^2 + 4$  prime  
 ↑  
 Not special !!

$$\text{Ex 5) } 27x^4 - 12 = 3(\underline{9x^4 - 4})$$

Factor

$$= 3(\overbrace{3x^2}^{\sqrt{9}} + \overbrace{2}^{\sqrt{4}})(\overbrace{3x^2}^{\sqrt{9}} - \overbrace{2}^{\sqrt{4}})$$

$$\text{Ex 6) } 16x^5 - 81x = x \underbrace{(16x^4 - 81)}_{\text{Factor}}$$

$$= x (4x^2 + 9) \underbrace{(4x^2 - 9)}_{\text{Factor}}$$

$$= x (4x^2 + 9) (2x + 3) (2x - 3)$$

Try This:

$$1) 9x^2 - 25y^2 = (3x + 5y) (3x - 5y)$$

$$2) 16 - 49x^2 = (4 + 7x) (4 - 7x)$$

$$3) 3x^4 - 3 = 3(x^4 - 1) \\ = 3(x^2 + 1) (x^2 - 1)$$

$$= 3(x^2 + 1) (x + 1) (x - 1)$$